

RADICALS

DEFINITION: any expression that has a square root, cuberoot, etc.

TYPES OF RADICALS: Square Roots $\sqrt{\quad}$, Cube Roots $\sqrt[3]{\quad}$, 4th Roots $\sqrt[4]{\quad}$, 5th Roots $\sqrt[5]{\quad}$, etc...

This year, we will focus on simplifying square roots and cube roots only.

SQUARE ROOTS

Simplify the following square roots.

1. $\sqrt{4} = 2$	2. $\sqrt{81} = 9$	3. $\sqrt{256} = 16$
4. $\sqrt{121} = 11$	5. $\sqrt{36} = 6$	6. $\sqrt{484} = 22$
7. $\sqrt{324} = 18$	8. $\sqrt{1} = 1$	9. $\sqrt{64} = 8$
10. $\sqrt{\frac{1}{16}} = \frac{1}{4}$	11. $\sqrt{\frac{9}{100}} = \frac{3}{10}$	12. $\sqrt{\frac{25}{49}} = \frac{5}{7}$

CUBE ROOTS

Simplify the following cube roots.

13. $\sqrt[3]{8} = 2$	14. $\sqrt[3]{-125} = -5$	15. $\sqrt[3]{729} = 9$
16. $\sqrt[3]{-1} = -1$	17. $\sqrt[3]{4096} = 16$	18. $\sqrt[3]{-343} = -7$
19. $\sqrt[3]{-64} = -4$	20. $\sqrt[3]{512} = 8$	21. $\sqrt[3]{1728} = 12$
22. $\sqrt[3]{-216} = -6$	23. $\sqrt[3]{1331} = 11$	24. $\sqrt[3]{-27} = -3$

$$\begin{array}{r} 2 \overline{) 162} \\ \underline{12} \\ 42 \\ \underline{40} \\ 20 \\ \underline{18} \\ 20 \\ \underline{18} \\ 20 \end{array}$$

Simplifying Non-Perfect Roots

NON-PERFECT SQUARE ROOTS: Use the perfect square numbers below to break the problem apart:

PERFECT SQUARES:

1, 4, 9, 16, 25, 36, 49, 64, 81, 100, etc...

Put the following in simplest radical form:		
1. $\sqrt{24} = \sqrt{4} \cdot \sqrt{6}$ $= 2\sqrt{6}$	2. $\sqrt{48} = \sqrt{16} \cdot \sqrt{3}$ $= 4\sqrt{3}$	3. $\sqrt{72} = \sqrt{9} \cdot \sqrt{8}$ $= 3\sqrt{8}$
4. $\sqrt{63} = \sqrt{9} \cdot \sqrt{7}$ $= 3\sqrt{7}$	5. $\sqrt{90} = \sqrt{9} \cdot \sqrt{10}$ $= 3\sqrt{10}$	6. $\sqrt{175} = \sqrt{25} \cdot \sqrt{7}$ $= 5\sqrt{7}$
7. $\sqrt{162} = \sqrt{81} \cdot \sqrt{2}$ $= 9\sqrt{2}$	8. $\sqrt{245} = \sqrt{49} \cdot \sqrt{5}$ $= 7\sqrt{5}$	9. $\sqrt{343} = \sqrt{49} \cdot \sqrt{7}$ $= 7\sqrt{7}$
10. $\sqrt{117} = \sqrt{9} \cdot \sqrt{13}$ $= 3\sqrt{13}$	11. $\sqrt{28} = \sqrt{4} \cdot \sqrt{7}$ $= 2\sqrt{7}$	12. $\sqrt{450} = \sqrt{25} \cdot \sqrt{18}$ $= 5\sqrt{9} \cdot \sqrt{2}$ $= 5 \cdot 3\sqrt{2} = 15\sqrt{2}$

NON-PERFECT CUBE ROOTS: Use the perfect cube numbers below to break the problem apart:

PERFECT CUBES:

1, 8, 27, 64, 125, 216, etc...

Put the following in simplest radical form:		
13. $\sqrt[3]{40} = \sqrt[3]{8} \cdot \sqrt[3]{5}$ $= 2\sqrt[3]{5}$	14. $\sqrt[3]{500} = \sqrt[3]{125} \cdot \sqrt[3]{4}$ $= 5\sqrt[3]{4}$	15. $\sqrt[3]{162} = \sqrt[3]{27} \cdot \sqrt[3]{6}$ $= 3\sqrt[3]{6}$
16. $\sqrt[3]{-16} = \sqrt[3]{-8} \cdot \sqrt[3]{2}$ $= -2\sqrt[3]{2}$	17. $\sqrt[3]{432} = \sqrt[3]{216} \cdot \sqrt[3]{2}$ $= 6\sqrt[3]{2}$	18. $\sqrt[3]{-320} = \sqrt[3]{-64} \cdot \sqrt[3]{5}$ $= -4\sqrt[3]{5}$
19. $\sqrt[3]{54} = \sqrt[3]{27} \cdot \sqrt[3]{2}$ $= 3\sqrt[3]{2}$	20. $\sqrt[3]{96} = \sqrt[3]{8} \cdot \sqrt[3]{12}$ $= 2\sqrt[3]{12}$	21. $\sqrt[3]{-875} = \sqrt[3]{-125} \cdot \sqrt[3]{7}$ $= -5\sqrt[3]{7}$
22. $\sqrt[3]{648} = \sqrt[3]{216} \cdot \sqrt[3]{3}$ $= 6\sqrt[3]{3}$	23. $\sqrt[3]{-297} = \sqrt[3]{-27} \cdot \sqrt[3]{11}$ $= -3\sqrt[3]{11}$	24. $\sqrt[3]{686} = \sqrt[3]{343} \cdot \sqrt[3]{2}$ $= 7\sqrt[3]{2}$