

8.AF.1 I-Step Review

Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms. Represent real-world problems using linear equations.

Coefficient is: numerical quantity placed before the variable

One Solution means only one value makes the equation work

Infinite Solutions means: any value works in the equation

No Solution means: no value works in the equation

Solve the following equations and explain its solution. Show all work.

<p>Solve:</p> $3x + 5 = -20$ $\begin{array}{r} -5 \quad -5 \\ \hline 3x = -25 \\ \frac{3x}{3} = \frac{-25}{3} \\ x = -8\frac{1}{3} \text{ or } -8.\bar{3} \end{array}$	<p>Solve:</p> $10 = -2z + 24$ $\begin{array}{r} -24 \quad -24 \\ \hline -14 = -2z \\ \frac{-14}{-2} = \frac{-2z}{-2} \\ z = 7 \end{array}$
<p>Solve:</p> $\frac{3}{4}x + 1 = 13$ $\begin{array}{r} -1 \quad -1 \\ \hline \frac{3}{4}x = 12 \\ \frac{4}{3} \cdot \frac{3}{4}x = 12 \cdot \frac{4}{3} \\ x = 16 \end{array}$	<p>Solve:</p> $5(x - 7) + 3 = 13$ $\begin{array}{r} 5x - 35 + 3 = 13 \\ 5x - 32 = 13 \\ +32 \quad +32 \\ \hline 5x = 45 \\ x = 9 \end{array}$
<p>Solve:</p> $3(2x + 9) = -5 - 2x$ $\begin{array}{r} 6x + 27 = -5 - 2x \\ +2x \quad +2x \\ \hline 8x + 27 = -5 \\ -27 \quad -27 \\ \hline 8x = -32 \\ \frac{8x}{8} = \frac{-32}{8} \\ x = -4 \end{array}$	<p>Solve:</p> $\frac{1}{2}(10k - 16) + 11 = -2$ $\begin{array}{r} 5k - 8 + 11 = -2 \\ 5k + 3 = -2 \\ -3 \quad -3 \\ \hline 5k = -5 \\ k = -1 \end{array}$
<p>Solve:</p> $4(3q + 10) = 6(2q - 9)$ $\begin{array}{r} 12q + 40 = 12q - 54 \\ -12q \quad -12q \\ \hline 40 = -54 \\ \emptyset \end{array}$ <p>No Solution</p>	<p>Solve:</p> $3x - 14 = 3(x - 5) + 1$ $\begin{array}{r} 3x - 14 = 3x - 15 + 1 \\ -3x \quad -3x \\ \hline -14 = -14 \checkmark \end{array}$ <p>Infinite solutions</p>
<p>Solve:</p> $2(12 - y) = 23 - (2y - 1)$ $\begin{array}{r} 24 - 2y = 23 - 2y + 1 \\ +2y \quad +2y \\ \hline 24 = 24 \checkmark \\ \infty \end{array}$	<p>Solve:</p> $4(2r + 3) = 15r - 11 + 1 - 7r$ $\begin{array}{r} 8r + 12 = 8r - 10 \\ -8r \quad -8r \\ \hline 12 = -10 \\ \emptyset \end{array}$

Solve:

$$\frac{3}{4}(20h - 4) = 8h - 45$$

$$15h - 3 = 8h - 45$$

$$\begin{array}{r} 15h - 3 = 8h - 45 \\ -8h \quad -8h \\ \hline 7h - 3 = -45 \\ +3 \quad +3 \\ \hline 7h = -42 \\ \frac{7h}{7} = \frac{-42}{7} \\ h = -6 \end{array}$$

Solve:

$$-2(3x - 5) = 2x + 10 - 8x$$

$$-6x + 10 = 2x + 10 - 8x$$

$$-6x + 10 = -6x + 10$$

$$\begin{array}{r} -6x + 10 = -6x + 10 \\ +6x \quad +6x \\ \hline 10 = 10 \checkmark \end{array}$$

**Consider the equation,

$$3(x - 2) = 3x - 2$$

Part A:

Determine whether the equation has one solution, no solutions, or an infinite number of solutions. Use words, numbers and/or symbols to justify your answer.

SHOW ALL WORK

$$\begin{array}{r} 3x - 6 = 3x - 2 \\ -3x \quad -3x \\ \hline -6 \neq -2 \end{array}$$

No Solutions because
-6 does not equal -2.

Part B:

Create a linear equation that has one solution. Include the variable on BOTH sides of the equal sign.

Equation: $2x + 4 = 4x - 6$

Part C:

Solve your equation from Part B.

SHOW ALL WORK

$$\begin{array}{r} 2x + 4 = 4x - 6 \\ -4x \quad -4x \\ \hline -2x + 4 = -6 \\ -4 \quad -4 \\ \hline -2x = -10 \\ \frac{-2x}{-2} = \frac{-10}{-2} \\ x = 5 \end{array}$$

Two fifths of the sum of a number and 4, plus -7 is 16. Write an equation that can be used to determine the number and then determine the number.

Equation: $\frac{2}{5}(x + 4) + (-7) = 16$

SHOW ALL WORK

Solution: $x = 53\frac{1}{2}$

$$\begin{array}{r} \frac{2}{5}(x + 4) + (-7) = 16 \\ \frac{2}{5}x + \frac{8}{5} + (-7) = 16 \\ \phantom{\frac{2}{5}x} + 7 \quad + 7 \end{array}$$

$$\begin{array}{r} \frac{2}{5}x + \frac{8}{5} = 23 = \frac{115}{5} \\ -\frac{8}{5} \quad -\frac{8}{5} \\ \hline \frac{2}{5}x = \frac{107}{5} \end{array}$$

$$\frac{5}{2} \cdot \frac{2}{5}x = \frac{107}{5} \cdot \frac{5}{2}$$

$$x = 53\frac{1}{2}$$

$\frac{23}{1/5}$